

The Price equation separates the total change into two component parts. The first part is the change that can be ascribed to the action of selection, and this takes the form of a statistical covariance between individuals' character values (z) and their relative reproductive success (w/\bar{w}). For example, if individuals with larger values of the character of interest tend to have more offspring, then the covariance is positive and selection acts to increase the population average value of the character. The remainder term takes the form of an expectation (arithmetic average) describing how offspring differ from their partners, and this is denoted the change due to transmission. If offspring are identical copies of their parents, then the transmission effect is zero and selection is the only factor involved in the evolution of the character. However, offspring will often differ from their parents, perhaps because of mutation, or because their genes are recombined in a new way, or because of a change in their physical, biological or cultural environment, and in this case the transmission effect is non-zero.

The importance of the Price equation lies in its scope of application. Although it has been introduced using biological terminology, the equation applies to any group of entities that undergoes a transformation. But despite its vast generality, it does have something interesting to say. It separates and neatly packages the change due to selection versus transmission, giving an explicit definition for each effect, and in doing so it provides the basis for a general theory of selection. In a letter to a friend, Price explained that his equation describes the selection of radio stations with the turning of a dial as readily as it describes biological evolution. Sadly, this general theory of selection remains undeveloped. Nevertheless, because of its generality and simplicity, Price's equation has been used to uncover fundamental processes in evolution and, as a meta-model, it allows comparisons and contrasts to be drawn between different models and methodologies. As such, it is an important conceptual aid that has led to the discovery of unexpected connections between different bodies of theory, has settled long running

controversies, and has helped to resolve semantic confusion.

Darwinism

The Price equation has most frequently been applied to biological evolution, and equation (1) appears to capture the Darwinian idea of the 'survival of the fittest'. Transmission effects aside, selection operates to favour those characters that are positively correlated with individual reproductive success. However, the modern theory of natural selection is framed in terms of changes in gene frequencies, and Price formulated this by focusing on the additive genetic component (g) of the character, rather than the actual phenotypic value (z). Discarding the genetic change due to transmission, the Price equation can be used to provide a formal statement of natural selection:

$$\Delta_s \bar{g} = \text{cov}(w/\bar{w}, g) = \beta_{w/\bar{w}, g} \text{var}(g). \quad (2)$$

Price found it illuminating to express natural selection as a product of its component factors: the regression (slope) of relative reproductive success against the genetic value of the individual ($\beta_{w/\bar{w}, g}$); and the genetic variation in the population ($\text{var}(g)$). This highlights the fact that natural selection operates when there are heritable differences between individuals with respect to some character that is correlated with reproductive success. Furthermore, because variances are never negative, any response to natural selection must be in the direction of increasing reproductive success (having the same sign as $\beta_{w/\bar{w}, g}$). The Price equation thereby captures the improving effect that natural selection has on biological populations.

Darwinism is a theory of the purpose as well as the process of adaptation. Darwin argued that because natural selection causes those characters that improve individual fitness to accumulate in biological populations, organisms will correspondingly appear as if designed to maximise their fitness. This appearance of design or agency makes biology unique among the natural sciences, and is the reason why the evolutionary literature abounds with intentional language — selfishness, strategies, conflicts of interest. But the issue of this almost magical appearance

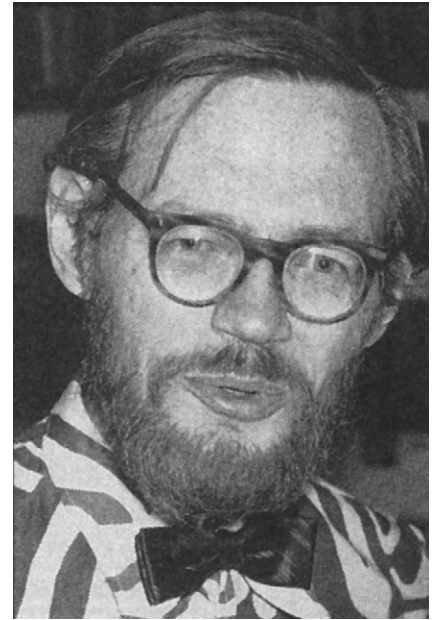


Figure 1. George R. Price.
Photograph taken in 1973. With thanks to Princeton University Press.

of agency has long been neglected by population geneticists, who have tended to obscure the role of the individual organism by focusing instead on genes and genotypes. Price's equation, in contrast, highlights the individual and its fitness, and links this to changes in gene frequency. For this reason, evolutionary theorist Alan Grafen has used the Price equation to establish mathematical links between population genetics and optimisation theory that formally justify the view of individual organisms as economic, fitness-maximising agents. In capturing both the process and purpose of adaptation, the Price equation forms the mathematical foundations of Darwinism.

Social evolution

Darwin argued that individuals should be favoured to behave in ways that improve their personal reproductive success. However, altruistic behaviour is common in the natural world, and this is difficult to reconcile with 'the survival of the fittest'. Recognising this problem, Darwin explained how certain characters could be favoured because they improve the reproductive success of one's relatives (kin selection), or else because they provide an overall benefit to the social group

